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## IMAGE RESTORATION TECHNIQUES: A COMPARATIVE STUDY BASED ON PERFORMANCE PARAMETERS

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**Abstract:** Image Restoration is a field of Image Processing which deals with recovering an original and sharp image from a degraded image using a mathematical degradation and restoration model. The purpose of image restoration is to estimate the original image from the degraded data. This paper attempts to undertake the study of Restored Blurred Images by using three types of deblurring techniques: Wiener filter, Regularized filter and Lucy Richardson, Blind Image Deconvolution Algorithm (BID). The analysis can be done on the basis of various performance metrics like PSNR(Peak Signal to Noise Ratio), MMSE(Mean Square Error).

**Keywords:** Peak Signal to noise ratio, Image Restoration, Degradation model, Richardson-Lucy algorithm, Wiener Filter.

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## INTRODUCTION

The improvement of pictorial information for human interpretation and processing of scene data for autonomous machine perception are the root application areas that had shown the interest in image processing field decades ago[1]. Image deblurring is usually the first process that is used in the analysis of digital images are produced to record or display use full information. Due to imperfections in the imaging and capturing process, however, the recorded image invariably represents a degraded version of the original scene [2]. There exists a wide range of different degradations, which are to be taken into account, for instance noise, geometrical degradations (pincushion distortion), illumination and color imperfections (under / overexposure, saturation), and blur [3]. Blurring is a form of bandwidth reduction of an ideal image owing to the imperfect image formation process [4].

It can be caused by relative motion between the camera and the original scene, or by an optical system that is out of focus. The field of image restoration (sometimes referred to as image deblurring or image deconvolution) is concerned with the reconstruction or estimation of the uncorrupted image from a blurred and noisy one. Essentially, it tries to perform an operation on the image that is the inverse of the imperfections in the image formation system.

### A. Degradation Model

Capturing an image exactly as it appears in the real world is very difficult if not impossible. In case of photography or imaging systems these are caused by the graininess of the emulsion, motion-blur, and camera focus problems. The result of all these degradations is that the image is an approximation of the original.

The above mentioned degradation process can adequately be described by a linear spatial model as shown in Figure 1. The original input is a two-dimensional (2D) image  $f(x,y)$ . This image is operated on by the system  $H$  and after the addition of  $n(x,y)$ , one can obtain the degraded image  $g(x,y)$ . Digital image restoration may be viewed as a process in which we try to obtain an approximation to  $f(x,y)$ , given  $g(x,y)$ , and  $H$  and after applying Restoration filters we obtain restored image  $f'(x,y)$ .

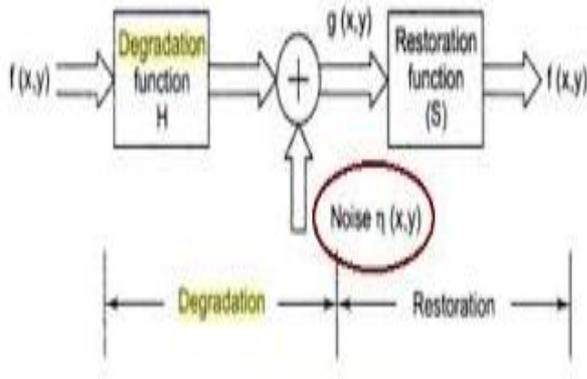


Fig 1: Degradation Model

## B. Blurring

In digital image there are 3 common types of Blur effects:

### 1) Average Blur:

The Average blur is one of several tools you can use to remove noise and specks in an image. We can use this tool when noise is present over the entire image [2]. This type of blurring can be distribution in horizontal and vertical direction and can be circular averaging by radius  $R$  which is evaluated by the formula:  $R = \sqrt{g^2 + f^2}$  (1) Where:  $g$  is the horizontal size blurring direction and  $f$  is vertical blurring size direction and  $R$  is the radius size of the circular average blurring.

### 2) Gaussian Blur

The Gaussian Blur effect is a filter that blends a specific number of pixels incrementally, following a bell-shaped curve [5]. Blurring is dense in the center and feathers at the edge. Apply Gaussian Blur filter to an image when you want more control over the Blur effect [6].

### 3) Motion Blur

The Many types of motion blur can be distinguished all of which are due to relative motion between the recording device and the scene. The Motion Blur effect is a filter that makes the image appear to be moving by adding blur in a specific direction [7]. The motion can be controlled by angle or direction (0 to 360 degrees or  $-90$  to  $+90$ ) and/or by distance or intensity in pixels (0 to 999), based on the software used [8].

## Point Spread Function (PSF)

Point Spread Function (PSF) is the degree to which an optical system blurs (spreads) a point of light [1]. The PSF is the inverse Fourier transform of Optical Transfer Function (OTF). In the frequency domain, the OTF describes the response of a linear, position-invariant system to an impulse. OTF is the Fourier transfer of the point (PSF) [9].

## 2. DEBLURRING TECHNIQUE

### A. Wiener Filter Deblurring Technique:

Norbert Wiener proposed optimal filter in a least-squares sense. Wiener filters are often applied in the frequency domain. These filters are comparatively slow to apply, since they require working in the frequency domain. Wiener Filtering is also a non blind technique for reconstructing the degraded image in the presence of known PSF. It removes the additive noise and inverts the blurring simultaneously. It not only performs the deconvolution by inverse filtering (highpass filtering) but also removes the noise with a compression operation (lowpass filtering). It compares with an estimation of the desired noiseless image. The input to a Wiener filter is a degraded image corrupted by additive noise. The output image is computed by means of a filter using the following expression:

$$f^{\wedge} = g * (f + n)$$

In equation,  $f$  is the original image,  $n$  is the noise,  $f^{\wedge}$  is the estimated image and  $g$  is the Wiener filter's response. The frequency domain expression for the Wiener filter is,

$$W(s) = H(s)/F_+(s), H(s) = F_x(s) \text{ eas } /F_x(s)$$

Where,  $F(s)$  is blurred image,  $F_+(s)$  causal,  $F_x(s)$  anti causal.

### B. Regularized Filter Deblurring Technique:

Regularized filtering is used effectively when constraints like smoothness are applied on their covered image and limited information is known about the additive noise. Regularized filter deblurs an image by using deconvolution function deconverge. The blurred and noisy image is restored by a constrained least square restoration algorithm that uses a regularized filter. Regularized restoration provides similar results as the Wiener filtering but it has a very different viewpoint. In regularized filtering less prior information is required to apply restoration. The regularization filter is often chosen to be a discrete Laplacian. This filter can be understood as an approximation of a Wiener filter.

### C. Lucy-Richardson Algorithm Technique:

This algorithm was introduced by W.H. Richardson (1972) and L.B. Lucy (1974). This is a Bayesian Based Iterative Method of image restoration. The R-L algorithm is the technique most widely used for restoring HST (Hubble Space Telescope) images. The standard R-L method has a number of characteristics that make it well-suited to HST data.

- The R-L iteration converges to the maximum likelihood solution for Poisson statistics in the data (Shepp and Vardi 1982), which is appropriate for optical data with noise from counting statistics.
- The R-L method forces the restored image to be non-negative and conserves flux both globally and locally at each iteration.
- The restored images are robust against small errors in the point-spread function (PSF).
- Typical R-L restorations require a manageable amount of computer time.

The Richardson–Lucy algorithm, also known as Richardson–Lucy deconvolution, is an iterative procedure for recovering a latent image that has been blurred by a known PSF.

$$C_i = \sum_j p_{ij} \cdot u_j$$

Where  $p_{ij}$  is the point spread function (the fraction of light coming from true location  $j$  that is observed at position  $i$ ),  $u_j$  is the pixel value at location  $j$  in the latent image, and  $C_i$  is the observed value at pixel location  $i$ . The statistics are performed under the assumption that  $u_j$  are Poisson distributed, which is appropriate for photon noise in the data. The basic idea is to calculate the most likely  $u_j$  given the observed  $C_i$  and known  $p_{ij}$ . This leads to an equation for  $u_j$  which can be solved iteratively according to:

$$u_j^{(t+1)} = u_j^t \sum_i \frac{C_i}{C_i} p_{ij}$$

Where

$$C_i = \sum_j u_j^{(t)} \cdot p_{ij}$$

It has been shown empirically that if this iteration converges, it converges to the maximum likelihood solution for  $u_j$ .

## D. Blind Image Deconvolution

As the name suggests, BID is a deconvolution technique that permits recovery of the target image from a single or set of blurred images in the presence of a poorly determined or unknown PSF. In this technique firstly, we have to make an estimate of the blurring operator i.e. PSF and then using that estimate we have to deblur the image. This method can be performed iteratively as well as non-iteratively. In iterative approach, each iteration improves the estimation of the PSF and by using that estimated PSF we can improve the resultant image repeatedly by bringing it closer to the original image. In non-iterative approach one application of the algorithm based on exterior information extracts the PSF and this extracted PSF is used to restore the original image from the degraded one. Blind deblurring method can be expressed by,

$$g(x, y) = \text{PSF} * f(x, y) + \eta(x, y)$$

Where  $g(x, y)$  is the observed image, PSF is Point Spread Function,  $f(x, y)$  is the constructed image and  $\eta(x, y)$  is the additive noise term.

## 3. PERFORMANCES PARAMETERS

In this section we discuss the two performance measuring parameters on which the above discussed techniques can be compared.

### 3.1 MMSE (Minimum mean square error)

In statistics and signal processing first error metrics, a minimum mean square error (MMSE) estimator is an estimation method which minimizes the mean square error (MSE) of the fitted values of a dependent variable, which is a common measure of estimator quality. Let  $x$  be a  $n \times 1$  unknown (hidden) random vector variable, and let  $y$  be a  $m \times 1$  known random vector variable (the measurement or observation), both of them not necessarily of the same dimension. An estimator  $\hat{x}(y)$  of  $x$  is any function of the measurement  $y$ . The estimation error vector is given by  $e = \hat{x} - x$ , and its mean squared error (MSE) is given by the trace of error covariance matrix,

$$MSE = \text{tr}\{E\{(\hat{x} - x)(\hat{x} - x)^T\}$$

Where, the expectation is taken over both  $x$  and  $y$ . When  $x$  is a scalar variable, then MSE expression simplifies to  $E\{(\hat{x} - x)^2\}$ . Note that MSE could equivalently be defined in other ways,

$$\text{tr}\{E\{ee^T\}\} = E\{\text{tr}\{ee^T\}\} = E\{e^T e\} = \sum_{i=1}^n E\{e_i^2\}$$

since

The MMSE estimator is then defined as the estimator achieving minimal MSE.

### 3.2 PSNR(Peak Signal to Noise Ratio)

Second of the error metrics used to compare the various image deblurring technique is the (Mean Square Error and PSNR) Peak Signal to Noise Ratio (PSNR). The MSE is the cumulative squared error between the compressed and the original image, whereas PSNR is a measure of the peak error. The mathematical formulae for the two are,

$$MSE = \frac{1}{MN} \sum_{y=1}^M \sum_{x=1}^N [I(x, y) - I'(x, y)]^2$$

$$PSNR = 20 * \log_{10} (255 / \text{sqrt}(MSE))$$

Where  $I(x, y)$  is the original image,  $I'(x,y)$  is the approximated version (which is actually the decompressed image) and M,N are the dimensions of the images.

### 4. CONCLUSION

In this paper, we discussed types of blurring, its causes and different deblurring techniques that restored image with great effect. All these techniques we can compare on the basis of two performance measure MMSR and PSNR. A lower value for MSE means lesser error, and higher value of PSNR as seen from the inverse relation between the MSE and PSNR. So, if you find a compression scheme having a lower MSE (and a high PSNR), you can recognize that it is a better one.

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