



INTERNATIONAL JOURNAL OF PURE AND APPLIED RESEARCH IN ENGINEERING AND TECHNOLOGY

A PATH FOR HORIZING YOUR INNOVATIVE WORK

A SLIDING MODE CONTROL ALGORITHM FOR ARTIFICIAL PANCREAS

NIRLIPTA RANJAN MOHANTY¹, PAUROOSH KAUSHAL², SURAJ GAUTAM³

1. Instrumentation & Control, D. Y. Patil College of Engineering Pune, India.
2. Instrumentation & Control, College of Engineering Pune, India.
3. Instrumentation & Control, Kurukshetra University, Kurukshetra, India.

Accepted Date: 05/03/2015; Published Date: 01/05/2015

Abstract: Artificial pancreas is simulated to handle type I diabetic patients under intensive care by automatically controlling the insulin infusion rate. In this paper, a sliding mode control via moving sliding surfaces is used to control blood glucose level in type I diabetic patient. The method is applied on the minimal model of Bergman subjected to an oral glucose tolerance test by applying a meal in form of a disturbance. The computer simulations are done using the mathematical model of the dynamics of blood glucose regulation in the blood system to manifest the theoretical analysis. In this control strategy, the sliding surface is moved, in contrast to the fixed surface of the conventional case. This is done so that the states of the model lie on the sliding surface at all times, and the dynamics is under control. The controller maintained the blood sugar level of the patient with the value of 4.5 mmol/l, when subjected to a meal disturbance. The control strategy has significantly lowered the risk of hypoglycemia/hyperglycemia of the patient.

Keywords: Type I diabetes; Sliding Mode Control; Bergman's minimal model

Corresponding Author: MS. NIRLIPTA RANJAN MOHANTY



PAPER-QR CODE

Access Online On:

www.ijpret.com

How to Cite This Article:

Nirlipta Ranjan Mohanty, IJPRET, 2015; Volume 3 (9): 674-681

INTRODUCTION

Type I diabetes mellitus or insulin- dependent diabetes mellitus is a chronic metabolic illness characterized by the absence or complete destruction of the pancreatic β -cells, which results in the rising of the blood glucose concentration above its normal level. The consequences of this disease are mostly long-term, such as kidney failure, blindness, nerve damage, heart attack, and ineffectiveness of the immune system [1]. Therefore type 1 patient need external insulin injection to assist glucose uptake and utilization.

The goal of our research is to investigate a control strategy to regulate blood glucose level in a type I diabetes mellitus. The controller or the “artificial pancreas” manipulates the insulin infusion rate in the blood such that the blood glucose level is maintained at normal level of 4.5 mmol/l which is reference glucose level [2]. The closed loop regulation strategy involves a glucose sensor in feedback loop that measures blood glucose level in blood of subject. This information is compared with reference glucose level, the result of which is passed to a controller. The controller implements sliding mode control strategy to controls the glucose level by manipulating the insulin dosage to be infused to patient to keep the blood glucose level in a stable range. A mechanical pump based on controller output, delivers the desired quantity of insulin. This closed-loop method of controlling the level of blood glucose in blood mimics the action of normal pancreas. [3][4] Figure 1 shows the block diagram of working of closed-loop control strategy for type 1 diabetic patient.

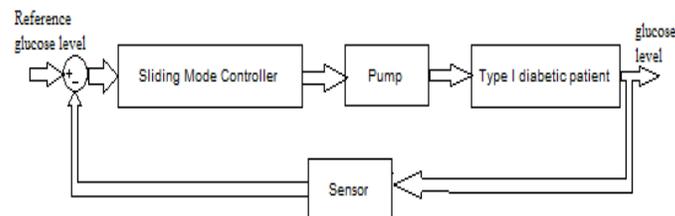


Fig 1. Closed loop control for blood glucose

In the study, the validity of minimal model of Bergman for type 1 diabetes is demonstrated and then Sliding Mode Control algorithm for controller action is discussed. The efficacy of the controller is shown by MATLAB simulation of type 1diabetic patient. The stimulated results show the control strategy resembles normal pancreas action and can be used for maintaining

blood glucose level for type 1 diabetic patient. Results with respect to controller performance and possible improvements are discussed.

MATHEMATICAL MODEL

The Bergman model provides a minimal model composed of 3 equations to describe the dynamics of the pancreas action [5]. These modeling equations are described below.

$$dG/dt = -P1 \cdot G - X(G + G_b) + D(t) \quad (1)$$

$$dX/dt = -P2 \cdot X + P3 \cdot I \quad (2)$$

$$dI/dt = -n(I + I_b) + U(t)/V_I \quad (3)$$

where, G is the plasma glucose concentration over basal (mmol/l), G_b is the basal plasma glucose (mmol/l), X is the generalized insulin variable for the remote compartment (1/min), I is the insulin concentration above basal (mU/l), I_b is the basal insulin level (mU/l), $D(t)$ is the external glucose input (mmol/min), $U(t)$ is the external insulin input (mU/min) and V_I is the insulin distribution volume (l). P_1 , P_2 , P_3 and n are the patient parameters. The parameters, P_1 , P_2 and P_3 , may be changed to represent different conditions. Type 1 diabetic patient individuals have the following parameters as $P_1=0$, $P_2=0.025$, $P_3=0.000013$ and for normal person, the values are $P_1=0.028$, $P_2=0.025$, $P_3=0.000013$ [6]. This model is linearized about the steady-state values of $G = I = X = D = 0$, $U=16.667$ mmU/min. A meal disturbance which is exogenous glucose infusion rate (mmol/min) given by the form $D(t)$. We use the oral glucose tolerance test as the exogenous glucose input of 50 grams glucose meal disturbance. The meal input is modelled by the following equation

$$D(t) = 1.157 \cdot \exp(-0.05 \cdot t) \quad (4)$$

Figure 2 shows the glucose concentration (mmol/l) of a healthy and a type 1 suffered person when meal disturbance is applied at $t=0$ min. It is easy to see that the glucose value of a healthy person is stabilized at the basal level. During about 2-3hours, the glucose concentration can be regulated to 4.5mmol/L. But the patient's glucose level still stays dangerously out of range. It can reach about 15.2mmol/l, and the hyperglycemia can induce various complications in long term. The aim is to design an optimal controller for insulin infusion, which can tightly control the blood glucose concentration in the normal level.

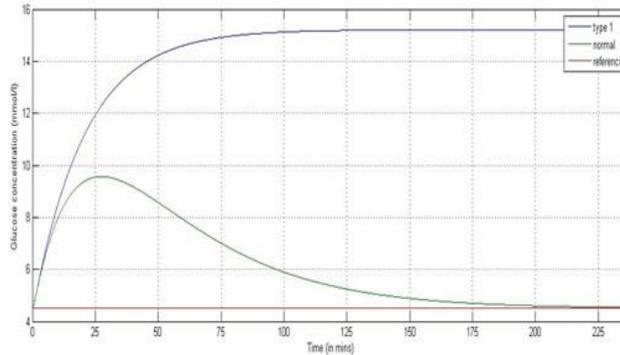


Fig. 2. Profile of glucose concentration during meal disturbance

CONTROLLER DESIGN

The steady state blood glucose level in the body is determined by how much insulin is present. In order to lower blood glucose level in the blood, insulin needs to be injected. Hence, the controller defines the insulin infusion rate, $U(t)$, based on the measured glucose concentration. Therefore blood glucose levels must be maintained in a tight range around the basal level, which matches the ideal blood glucose levels. To achieve this, Sliding Mode Control is introduced to control the insulin infusion rate.

Sliding Mode Control

The study of sliding mode control has gained popularity in recent years as a methodology for controlling nonlinear and linear systems with modeling uncertainties and external disturbances. The most important step of the control design is the construction of the sliding surface S which is expected to response desired control specifications and performance. The trajectories are enforced to lie on the sliding surfaces [7]. This section discusses the design of sliding surface for bergman minimal model with meal as a perturbation. The model is represented in discrete state space matrices as

$$x = Ax(t) + Bu(t) + \Delta A x(t) + \Delta B u(t) + D(x,t) \quad (5)$$

$$Y = Cx(t) \quad (6)$$

where A, B and C are known matrices or the patient parameters. $\Delta A, \Delta B$ are uncertainties in parameter values, $D(x,t)$ is an disturbance or input meal signal to the system, $x(t)$ is the state vector and $u(t)$ is control input.

Assumptions

The uncertainties ΔA , ΔB and the disturbance $D(x, t)$ satisfy the matching conditions given by:

$$\Delta A = B^*D \quad (7)$$

$$\Delta B = B^*E \quad (8)$$

$$D(x, t) = B^*v(x,t) \quad (9)$$

where D and E are unknown matrices of appropriate dimensions and $v(x,t)$ is an external disturbance. The system can now be written as described by,

$$\dot{x} = Ax(t) + Bu(t) + Be(x,t) \quad (10)$$

where $e(x,t) = Dx + Eu + v(x,t)$ are referred as lumped uncertainty in the system. Let the sliding surface for the system be defined as follows

$$\sigma = S^*x \quad (11)$$

The attractivity of the surface is assured by enforcing the sliding surface attractivity condition, as given by

$$\sigma^* \dot{\sigma} \leq 0 \quad (12)$$

The control signal is proposed as:

$$u = u_{eq} + u_n \quad (13)$$

where u_{eq} takes care of known parameters and u_n takes care of uncertain and disturbance term.

Choosing u_{eq} and u_n such that the sliding surface condition is met and are given as:

$$u_{eq} = (SB)^{-1} * (SAx + \alpha * \sigma(0) * \exp(-\alpha t)) \quad (14)$$

$$u_n = \rho * \text{sign}(\sigma SB) / (1 - \beta) \quad (15)$$

where α indicates the rate of reaching sliding surface from any initial condition, $\sigma(0)$ is the sliding surface at initial point of the system, ρ is the maximum possible value of lumped uncertainty, and β is a positive number less than 1.

Simulation

Bergman's model comes with an artificial pancreas has two inputs, the ingested glucose in plasma after a meal reflected by the disturbance function $D(t)$ and insulin from an external injection $u(t)$ that plays the controllers role. The performance of the control algorithm investigated above was tested for a standard meal disturbance with about four hour duration for type 1 diabetic patient. The actual input signal the insulin infusion rate $U(t)$ is controlled by sliding mode controller. Figure 3 shows control of blood glucose concentration to the normal level. The controller action is seen when meal disturbance is given, the glucose concentration can reach about 10 mmol/l and then it is stabilized at the basal level finally in about 4 hours. Figure 4 and Figure 5 illustrates the remote compartment insulin utilization and plasma insulin concentration respectively. The response time is suitable and matches with physiological regulation system. Figure 6 gives glucose concentration profiles of normal and sliding mode controlled type I diabetic patient during meal disturbance. The profile of type I approaches the normal person response very closely. The simulation can be implemented on hardware and accepted by the clinical research.

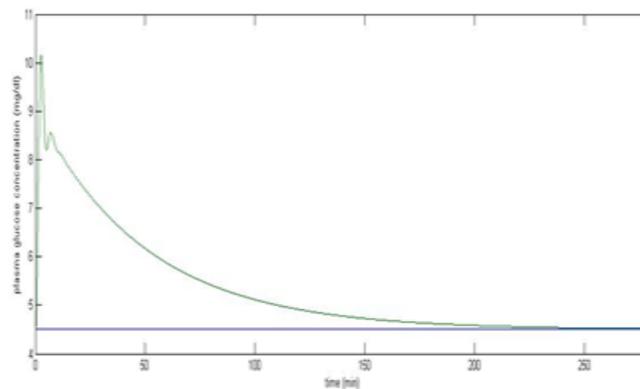


Fig. 3. plasma glucose profile of type I patient with control action

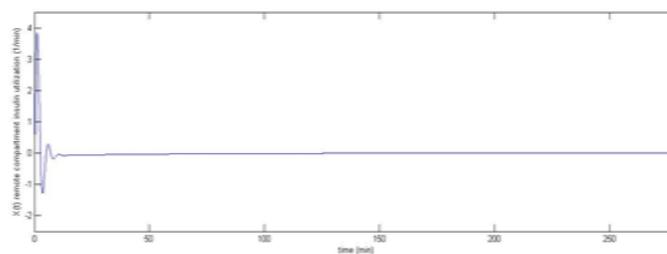


Fig. 4. remote compartment insulin utilization during controller action

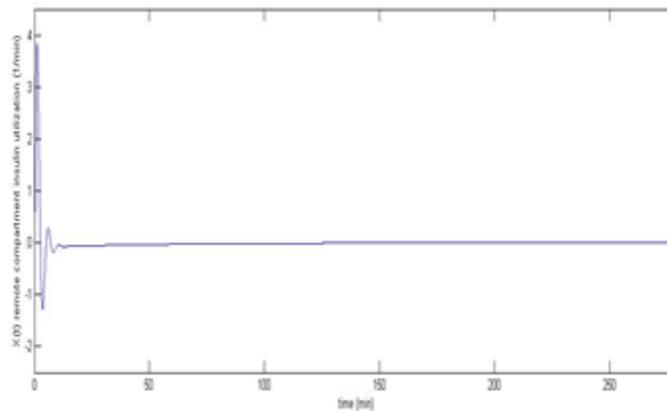


Fig. 5. Comparison of plasma glucose profiles of healthy and type I diabetic

CONCLUSION

The case study presented a robust control strategy to regulate glucose-insulin system for type I diabetic patient. The controller is very effective in the blood glucose regulation. It can control the glucose concentration and the regulation of profile approaches the normal person. There is no instance of hyperglycemia or hypoglycemia during regulation of plasma glucose level. Future work would be implementing the controller on hardware and designing of insulin pump. It can believe that the work is suitable for applications related to human body where precision is of great concern.

REFERENCES

1. C. V. Doran, J.G. Chase, G.M. Shaw, K.T. Moorhead, and N.H. Hudson, "Derivative weighted active insulin control modeling and clinical trials for ICU patients", *Medical Engineering & Physics*, vol. 26, issue 10 pp. 855-866, 2004.
2. Weijiu Liua, Fusheng Tang, "Modeling a simplified regulatory system of blood glucose at molecular levels", *Journal of Theoretical Biology*, vol. 252, pp 608–620, 2008.
3. Z-H Lam, K-S Hwang, J-Y Lee, J-G Chase, G-C Wake, "Active insulin infusion using optimal and derivative weighted control", *Medical Engineering & Physics*, vol. 24, pp. 663–672, 2002.
4. Chengwei Li, Ruiqiang Hu, "Fuzzy-PID Control for the regulation of blood glucose in diabetes" *Global Congress on Intelligent Systems IEEE Computer Society*, pp 170-174, 2009.

5. R. N. Bergman, L.S. Philips, C. Cobelli, "Physiological evaluation of factors controlling glucose tolerance in man," J.Clin.Znvest., vol 68, pp. 1456-1467,1981
6. Sandra M. Lynch, B. Wayne Bequette, "Estimation-based model predictive control of blood glucose in type I diabetics: a simulation study" IEEE 27th Annual Northeast Bioengineering Conference, pp 79-80, 2001.
7. S. Tokat, I. Eksin, M. Guzelkaya, "Sliding mode control using a nonlinear time-varying sliding surface" 10th Mediterranean Conference on Control and Automation, July 9-12, 2002