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## DESIGN OF HIGH SPEED ALU USING REVERSIBLE LOGIC GATES BASED ON VEDIC MATHEMATICS

SHRUTI D. KALE, GAURI N. ZADE

DATTA MEGHE COLLEGE OF ENGINEERING TECHNOLOGY & RESEARCH CENTRE WARDHA

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**Abstract-** In modern times reversible logic fascinate notable attention to produce something better in certain fields like nanotechnology, quantum computing and low power design. This work is devoted for the design of an Arithmetic module with high speed and low power dissipation. In this project addition and multiplication are considered as main functions, because these functions affect the speed of operation and causes power dissipation. Reversible logic has shown potential to have extensive applications in emerging technologies such as quantum computing, optical computing, DNA computing to produce almost zero power dissipation under ideal conditions. The speed of ALU has been improved using ancient system of mathematics which is Vedic mathematics. It has a unique technique of calculations based on 16 Sutras and 13 Upa-sutra. The designing using reversible logic reduce power dissipation in terms of TRLIC. In this project both technic utilized and designed circuit achieved high speed and less power dissipation as resultant TRLIC is optimized.

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Corresponding Author: SUKANTI B. MARDOLKAR

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## INTRODUCTION

The design of the ALU is difficult part of the processor and modifications towards speed up instruction handling are continually being developed. Today nano computing attracts more interest due to ability of processors to perform complex and challenging processes with higher speeds. Processors speed greatly depends on multiplier, due to this regard multiplier unit employ Vedic mathematics sutras in computation algorithms which will reduce the complexity, execution time, area etc.

Along with Vedic mathematics Reversible logic has received great attention in the past years due to its ability to reduce the power dissipation which is the main requirement in low power digital design.

Conventional logic circuits dissipate a significant amount of energy because bits of information are erased during the logic operations. Thus, if logic gates are designed such that the information bits are not destroyed, the power consumption can be decrease dramatically. The information bits are not lost in case of a reversible computation.

### System Model Description

#### Reversible Logic gates:-

In the recent past, Reversible logic has more demand due to its less heat dissipating characteristics. Many researches have been performed with the efforts on design and synthesis of efficient reversible logic circuits. Reversibility shows that no information about the computational states can lose, so we can recover any previous stage by computing backwards or uncomputing the results. This is termed as logical reversibility. It has been proved that, any Boolean function can be executed logically using reversible gates. The design of reversible logic circuits consider following points to achieve an optimized circuit.

They are:-

- i) Fan-out is not allowed.
- ii) Loops or feedbacks are not allowed.
- iii) Garbage outputs must be less in numbers.
- iv) Reduced delay.

The basic reversible logic gates which are useful in the designing of Urdhva Tiryagbhyam Multiplier (UTM) module are Feynman gate, Peres gate, Toffoli gate, HNG gate and BVPPG gate are shown in above figure (1). Feynman gate is the 2x2 gate with quantum cost 1, used for fan-out purpose as well as complementing. Peres gate is the 3x3 gate with quantum cost 4. Toffoli gate is the 3x3 gate with quantum cost 5. HNG gate is the 4x4 gate with quantum cost 6 and BVPPG is 5x5 gate along with quantum cost 10.

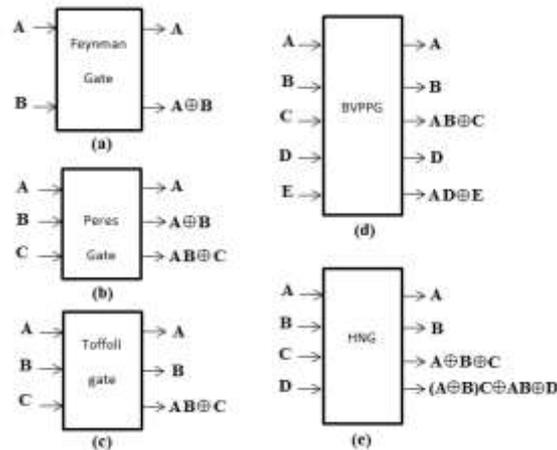


Figure 1: Reversible Logic Gates

### Optimized Parameters for Reversible Logic Circuits:-

**Constant Inputs (CI):-** Number of inputs that are to be sustained constant at either '0' or '1'.

**Garbage Outputs (GO):-** Number of outputs that are not used in the synthesis of a given function. These are vital part of the reversible designing.

**Gate Count (GC):-** Number of gates required for the design of function.

**Quantum Cost (QC):-** It is the cost of the circuit in terms of the cost of a basic gate. Quantum cost calculation depends on the number of gates required to realize the circuit.

**Total Reversible Logic Implementation Cost (TRLIC):-** TRLIC is the summation of Constant Inputs (CI), Garbage Outputs (GO), Gate Count (GC) and Quantum Cost (QC). It is given by-  

$$TRLIC = \sum (CI + GO + GC + QC)$$

### Urdhva Tiryagbhyam:-

The formula simply means: "Vertically and crosswise"

Urdhva Tiryagbhyam sutra is a general multiplication formula applicable to all cases of multiplication. The digits on the both sides of the line are multiplied and added with the carry from the previous step. This generates one of the bits of the result and a carry. This carry is added in the next step and hence the process goes on. If more than one line are there in one step, all the results are added to the previous carry. In each step, least significant bit acts as the result bit and all other bits act as carry for the next step. Initially the carry is taken to be zero.

### 2x2 Bit UTModule:

The method is explained below for two, 2 bit numbers A and B where  $A = a_1a_0$  and  $B = b_1b_0$  as shown in Figure 2. Firstly, the Least Significant Bits (LSB) are multiplied which gives the LSB of the final product (vertical). Then, the LSB of the multiplicand is multiplied with the next higher bit of the multiplier and added with, the product of LSB of multiplier and next

higher bit of the multiplicand (crosswise). The sum gives second bit of the final product and the carry is added with the partial product obtained by multiplying the most significant bits to give the sum and carry. The sum is the third corresponding bit and carry becomes the fourth bit of the final product.

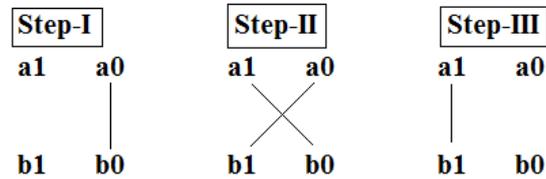


Figure 2: The Vedic Multiplication Method for Two 2-Bit Binary Numbers

The reversible logic design for 2-bit vedic multiplication is possible by the use of four Toffoli gates and Two Peres gates [9] is as shown in figure (3).

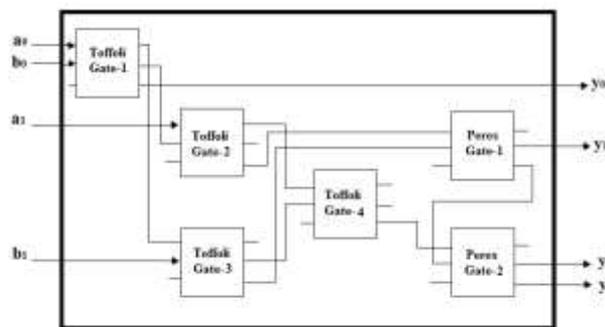


Figure 3: 2x2 Bit UTM Module.

The circuit shown in figure (3) has total quantum cost of 28, number of garbage outputs 6 with constant inputs 6 and gate count is 6. Including everything the performance of UTM is scaled up and optimized.

But further optimization is possible with the use of BVPPG gate, three Peres gates and one Feynman gate. The Modified 2X2 Vedic multiplier module is implemented using a reversible logic gate which is shown in Figure (4). This design has total quantum cost of 23, number of gates required to design multiplier is 5 along with total garbage outputs are 5 and constant inputs are 5.

**5-Bit Ripple Carry Adder Module:**

The 5-bit adder circuit form with four HNG gate and one Peres gate is discussed in Figure (5). Here A0B0 is given to Peres gate which acts as half adder, produce output S0 (sum) and carry forward to HNG gate which acts as full adder. The resultant output S1 (sum) and carry from first HNG gate forward to next HNG gate, like wise S2, S3 and S4 generated.

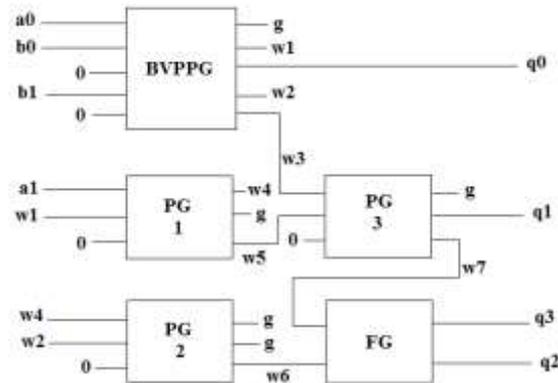


Figure 4: Modified 2x2 Bit UTM.

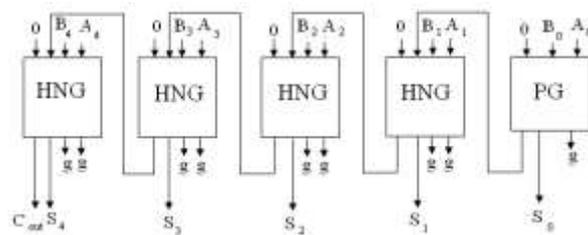


Figure 5: 5-Bit Ripple Carry Adder

5-Bit ripple carry adder design has total quantum cost of 28, number of gates are 5, with total garbage outputs are 9 and constant inputs are 5.

#### 4-Bit Ripple Carry Adder Module:

The 4-bit adder circuit form with four HNG gate is as shown in Figure (6). Here HNG gate which acts as full adder, the resultant output  $S_0$  (sum) and carry forward to next HNG gate, like wise  $S_1$ ,  $S_2$  and  $S_3$  generated.

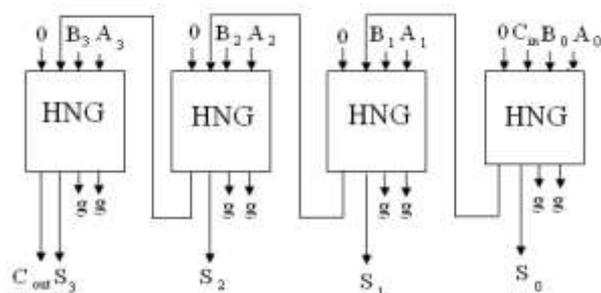
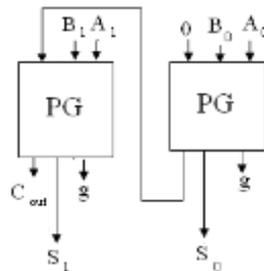


Figure 6: 4-Bit Ripple Carry Adder

4-Bit ripple carry adder design has total quantum cost of 24, number of gates are 4, with total garbage outputs are 8 and constant inputs are 4.

**2-Bit Ripple Carry Adder Module:**

The 2-bit adder circuit form with two Peres gate is as shown in Figure (7). Here Peres gate which acts as half adder, the resultant output  $S_0$  (sum) and carry forward to next Peres gate, like wise  $S_1$  generate.

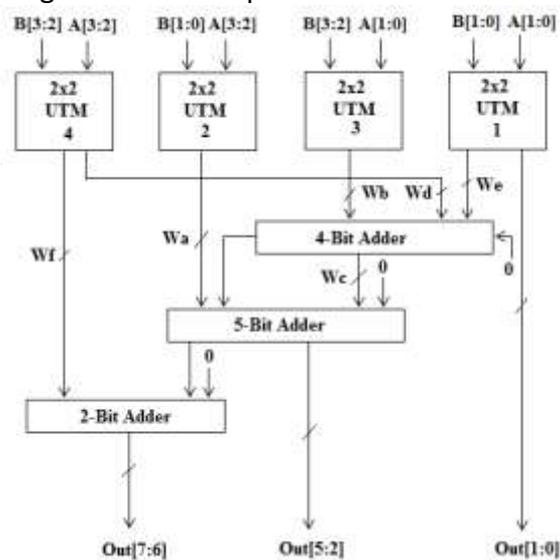


**Figure 7: 2-Bit Ripple Carry Adder**

2-Bit ripple carry adder design has total quantum cost of 8, number of gates are 2, with total garbage outputs are 2 and single constant input.

**Vedic Multiplier for 4x4 Bit UTM Module:**

The circuit of 4x4 bit UTM consist four 2x2 UTM, one 5-bit carry ripple adder, one 4-bit carry ripple adder and one 2-bit carry ripple adder as shown in Figure (8). The resulted Vedic multiplier can be used to reduce delay. Interestingly, 8x8 Vedic multiplier modules are implemented easily by using four 4x4 multiplier modules.



**Figure 8: 4x4 Bit UTM Module**

Observation

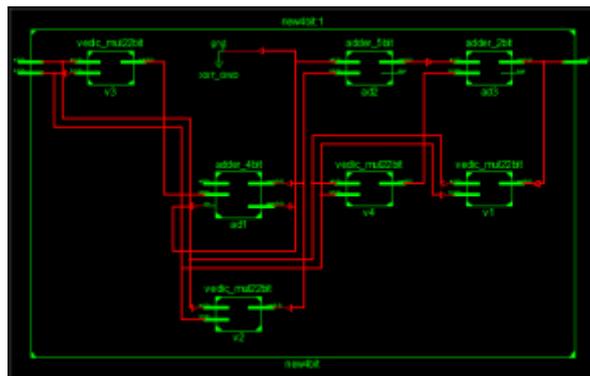


Figure 9: RTL Schematic of 4x4 Bit UTM Module

The RTL Schematic view of internal architecture of 4x4 UTM is as shown in Figure (9).



Figure 10: Simulation Result of 4x4 Bit UTM Module.

To verify the result, assume two 4-bit numbers as, a=10 (1010) and b=10 (1010) the resultant output is of 8-bit Out=100 (01100100). The simulation results for this case are shown in Figure (10) and corresponding design summary table is given in Table 1.

Table 1: Design Summary of 4x4 Bit UTM

| Logic Utilization     | Used                          | Available | Utilization |
|-----------------------|-------------------------------|-----------|-------------|
| Number of Slices      | 23                            | 27288     | 0%          |
| Number of IOs         | 16                            |           |             |
| Number of bonded IOBs | 16                            | 296       | 5%          |
| Delay                 | 9.155ns (Levels of Logic = 6) |           |             |

RESULT & COMPARISON

The Reversible Multiplier Unit attains a significant improvement in performance with Vedic calculations and reversible way of design. The important constraints for any reversible logic design consist of-

- i) Reversible logic circuits should have minimum quantum cost.
- ii) The design can be optimized so as to produce minimum number of garbage outputs.

iii) The reversible logic circuits must use minimum number of constant inputs.  
iv) The reversible logic circuits must use a minimum number of reversible gates.  
Meanwhile TRLIC is summation of all these factors; it is estimable to have least value of TRLIC. The comparison of 4x4 bit multiplier design is given in Table 2.

**Table 2: Comparison of 4x4 Bit Multiplier Design with Previous Designs**

| Multiplier Designs          | No. of Gates | Constant Inputs | Garbage Outputs | Quantum Cost | TRLIC | Unit Delay |
|-----------------------------|--------------|-----------------|-----------------|--------------|-------|------------|
| Reversible Multiplier Unit  | 31           | 37              | 36              | 152          | 256   | 31         |
| Rakshith Saligram et al [7] | 33           | 33              | 43              | 164          | 273   | 33         |
| Rakshith Saligram et al [7] | 33           | 33              | 39              | 168          | 273   | 33         |
| Shruti Kale et al [9]       | 37           | 27              | 24              | 189          | 277   | 37         |
| Majid Haghparast et al [10] | 52           | 52              | 52              | 152          | 368   | 52         |
| Masoumeh Shams et al [11]   | 52           | 56              | 56              | 208          | 372   | 52         |
| H. P. Sinha et al [12]      | 44           | 56              | 64              | 236          | 400   | 44         |
| H. Thapliyal et al [13]     | 53           | 58              | 58              | 234          | 403   | 53         |
| S. Bobazadeh et al [14]     | 48           | 52              | 64              | 244          | 408   | 48         |

### Conclusion and Future scope

Along with reversible logic Vedic mathematics is a gift given to this world by the ancient sages of India. Reversible logic gates reduce power dissipation thus reversible ALU consume less power and Vedic mathematics which is well known for high speed operation, resulting ALU achieves high speed. By utilizing beneficial features of low power and high speed has been implemented for design of ALU. On comparing with previous multiplier design, the project design found more optimized.

An important aspect of designing circuits using reversible logic gates is to reduce the power dissipation which directly affects TRLIC. Future work could be extended to optimizing TRLIC by minimizing the garbage outputs and constant inputs in the circuit.

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